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An Algorithm for the Integrated Scheduling Problem of a Container Handling System Within a Container Terminal

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Currently, there has been an exponential increase in container volume shipment within intermodal transportation systems. Container terminals as part of the global ports represent important hubs within the systems. Thus, the need to improve the operational efficiency is the most important issue for container terminals from an economic standpoint. In order to increase the efficiency of operations, the development of optimization models and mathematic algorithms is critical in finding an optimal solution. The objective of this study is to evaluate the optimum solution to find the proper number of Yard Trailers (YTs) with the minimal cost for the container terminals. This study uses the Dynamic YTs operation's method as a background for modeling. A mathematical model with various constraints related to the integrated operations among the different types of handling equipment is formulated. This model takes into consideration both serving time of different types of cranes, and cost reduction strategies by decreasing use of YTs with the specific objective of minimum total cost including utilization of YTs and vessel berthing time. A heuristic algorithm combined with Monte Carlo method and Brute-force search are employed. The Monte Carlo method is proposed to generate vast random numbers to replicate simulation. The Brute-force search is used for identifying all potential cases specific to the conditions of this study. Some preliminary numerical test results suggest that this method is good for use in conjunction with simulation of container terminal operations.

Modeling and Simulation on the Yard Trailers Deployment in the Maritime Container Terminal

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Abstract

In recent years, there has been an exponential increase in container volume shipment within intermodal transportation systems. Container terminals as part of the global port system represent important hubs within this intermodal transportation system. Thus, the need to improve the operational efficiency is the most important issue for container terminals from an economic standpoint.

The objective of this study is to evaluate the solutions to find the proper number of Yard Trailers (YTs) with the minimal cost for the container terminals. This study simulates the YTs' operations under the dynamic YTs operations' method and takes into consideration both serving time of quay cranes and yard cranes, and cost reduction strategies by decreasing use of YTs with the specific objective of minimum total cost including utilization of YTs and vessel in the berth. In addition, The Monte Carlo method is proposed to generate vast random numbers to replicate simulation for real cases. The Brute-force search is used for identifying all potential cases specific to the conditions of this study.

Some preliminary numerical test results suggest that this method is good for use in conjunction with simulation of container terminal operation. The expected outcome of this research is a solution to obtain the best feasible number of YTs for transporting containers with a minimum cost; thus, improving the operational efficiency in a container terminal.

Objective

- Evaluate the best feasible solution to find the proper number of Yard Trailers (YTs) with the minimal cost for the container terminals
- Develop a mathematical model with various constraints related to the integrated operations among the different types of handling equipment to look for the solutions to improve the operational efficiency

Background and Problem Statement

The performance of container terminal is very important to the intermodal freight transportation, and the container operations can be grouped in to three parts:

- Container Assignment
- Resource allocation: Quay Cranes, Yard facilities
- Logistics and Transportation

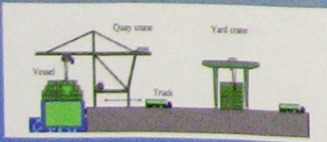


There has been an exponential increase in container volume shipment within intermodal transportation systems

From an economic standpoint, the need to improve the operational efficiency is the most important issue for container terminals

The full use of all loading and unloading equipment is necessary in order to increase revenue

Yard Trailers (YTs) are important to improve efficiency and reduce cost for unloading and loading operations



Methodology

① Develop a mathematical model

- The dynamic YTs operation's method (inter-ship method) is used as a background for modeling
- The first principle is the mooring time of the unloading vessel (as short as possible)
- The second principle is to find an appropriate total # of trailers that can minimize the total cost (vessel mooring costs and vehicle costs)

② Develop an algorithm to replicate the simulation and look for the best feasible solution

③ The model's performance is tested with a MatLab simulation

Assumptions

① Cost Functions

$$MC(k) = \sum_{i=1}^N MC_i \max_i t_i, \quad VC(k) = \sum_{i=1}^N VC_i \cdot t_i$$

② YTs Analysis

$$d_i = d_1 + d_2 + d_3 + |x_i - x_i^0| + |y_i - y_i^0| + |x_i^0 - x_i^1| + |y_i^0 - y_i^1| + |x_i^1 - x_i^2| + |y_i^1 - y_i^2|$$

$$t_i = \frac{d_i}{v} + Y_{d_i} + Y_{d_i} + Q_{d_i}, \quad k_{ij} = t_i / Q_{d_i}, \forall i \in L, j \in I, \quad 0 \leq k \leq \max_{i \in L} |Q_{d_i}|, \forall i \in L, j \in I$$

③ Objective Function

$$Z = MC(k) + VC(k) \quad \min_{k \geq 1} Z$$

④ Constraints

$$0 \leq x_i \leq m_i$$

$$0 \leq x_j \leq m_j$$

$$0 \leq y_i \leq n_i$$

$$0 \leq y_j \leq n_j$$

$$N^+ = N^-$$

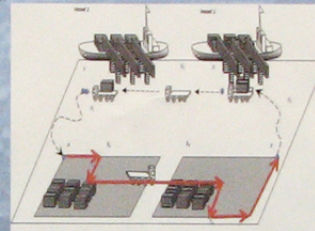
$$o_c - o_{c+1} \geq 0, \quad \forall c, c+1 \in C$$

Variables

- Z: the total cost
- MC(k): the cost of mooring in the berth of the unloading vessel (S)
- VC(k): the cost of YTs in use (S)
- d_i : the distance of the i^{th} circle of the i^{th} YT
- t_i : the time of the i^{th} YT
- k_{ij} : the number of YTs in use during the i^{th} circle of the j^{th} YT
- P_i : the random position in the yard for storage: $P_i = (x_i, y_i) | (x_i, y_i) \in S^A \wedge (x_i, y_i) \text{ is empty}$
- P_j : the random position in the yard for loading to the loading vessel: $P_j = (x_j, y_j) | (x_j, y_j) \in S^B \wedge (x_j, y_j) \text{ has the loading container}$
- $O_{c+1} - o_c$: the value of the loading container c and $c+1$
- k : the proper number of YT in use

Parameters

- V_{d_i} : the unit time of the operation of the YC for unloading (min*/per container)
- V_{d_j} : the unit time of the operation of the YC for loading (min*/per container)
- Q_{d_i} : the unit time of the operations of the QC for loading (min*/per container)
- Q_{d_j} : the unit time of the operations of the QC for loading (min*/per container)
- v : the velocity of the YTs (m/min)
- MC_i : the unit cost of mooring in the berth (S/min)
- VC_i : the unit cost of the YT in use (S/min*/car)
- N : the number of unloading containers from the unloading vessel
- N^+ : the number of loading containers from the loading vessel



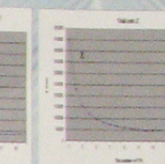
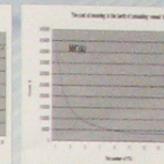
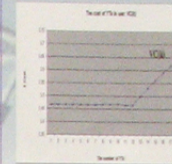
Numerical Test Results

Input Data

Case	YC	QC	YT
1	100	4	10
2	100	4	10
3	100	4	10
4	100	4	10
5	100	4	10
6	100	4	10
7	100	4	10
8	100	4	10
9	100	4	10
10	100	4	10
11	100	4	10
12	100	4	10
13	100	4	10
14	100	4	10
15	100	4	10
16	100	4	10
17	100	4	10
18	100	4	10
19	100	4	10
20	100	4	10

The mean value after 10000 simulation runs

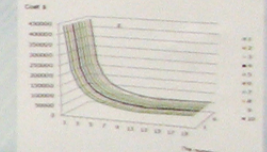
Case	MC(k)	VC(k)	Z
1	10000	10000	20000
2	10000	10000	20000
3	10000	10000	20000
4	10000	10000	20000
5	10000	10000	20000
6	10000	10000	20000
7	10000	10000	20000
8	10000	10000	20000
9	10000	10000	20000
10	10000	10000	20000
11	10000	10000	20000
12	10000	10000	20000
13	10000	10000	20000
14	10000	10000	20000
15	10000	10000	20000
16	10000	10000	20000
17	10000	10000	20000
18	10000	10000	20000
19	10000	10000	20000
20	10000	10000	20000



Sensitivity Analysis

① Container Configuration

- Choose 10 simulation results randomly:
- Before best feasible number of YTs is reached, there are very small differences in cost between 10 simulations
- After this point, cost is the same



② Change the ratio of the unit cost of the unloading vessel in the berth and the unit cost of the YTs

$$MC_i = [5, 30] \quad VC_i = [0.2, 1]$$

③ Change the ratio of the unloading volume and the number of QCs

The work load of a QC = [200, 600]; The QC are assigned for each vessel = [2, 6]

④ Change the ratio of the unit time of the QC for unloading and loading

Q _u /Q _l (min)	The number of YTs	MC(k)	VC(k)	Z
1.5-3	12	21960	2988.4	47908.4
2-3	12	16842.2	2833.36	41168.94
1.5-3	18	21868.8	2616	9059.8
1.5-2.5	18	28923	2918	16619.8

Unloading container QC for unloading	The number of YTs	MC(k)	VC(k)	Z	Min
15-2	12	28257	3766.26	120481.1	756
15-3	12	28257	3862.6	120481.1	680
15-4	12	28268	3918.2	120481.2	688
15-2-5	12	28247.3	3853.84	120481.2	678
15-3-5	12	18984.1	3824.81	117981.2	642
15-4-5	12	28253.1	3523.2	120481.2	678
15-4-5	12	27318.9	3714.84	117981.2	624
15-2-5	12	28262.6	3884.84	120481.2	678
15-3-5	12	28262.6	3884.84	120481.2	678
15-4-5	12	28262.6	3884.84	120481.2	678

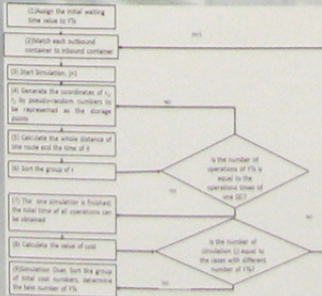
VC _i /MC _i	The number of YTs	MC(k)	VC(k)	Z
0.5-2.0	12	27861	1611.5	1657
0.5-1.5	12	18018.4	1378.26	33503.26
0.5-1.5	12	18018.8	1753.41	33633.44
1.5	12	6013.08	1438.67	64463.72
0.5-1.5	13	17079	1623.80	15784.80

Results Summary

- The configuration of the containers has negligible affect on the cost
- Changing the unit cost (with in a valid range) has no affect the optimal number of YTs
- Changing the load on QC_u (with in a valid range) has no affect the optimal number of YTs
- Changing the unit operation time of the QC for unloading (with in a valid range) has a marginal impact on the optimal number of YTs
- The unit costs will dominate the relationship and the trend of the two cost functions

Solution Algorithm

Monte Carlo Method will be employed to replicate the simulation; Brute-force Search will be used to look for the best feasible solution.



Conclusion

① Contributions

- A mathematical model is developed to formulate the YTs' deployment
- An algorithm is developed to replicate the simulation to search for the best feasible number of YTs

② Limitations

- Data Collection
- Model Development

③ Future Research

- Optimization of yard storage policy and integrating unloading and loading operations schedules could be considered